

**TOPIC: FRACTION AND DECIMAL**

# SETS

A set is a collection of well defined distinct objects.

The objects of the set are called elements.

Sets are denoted by  
Capital letters

Sets use "curly" brackets

$$A = \{1, 3, 2, 5\}$$

$$n(A) = 4$$

The number of elements  
in Set A is 4

$$3 \in A$$

3 is an element of A

$$7 \notin A$$

7 is not an element of A

$\{1, 2, 3, 5\}$

We never repeat elements in a set.

Sets can be represented by two methods:

**Rooster or Tabular form:**

In this the elements are separated by commas.

e.g. set A of all odd natural numbers less than 10.

$A = \{1, 3, 5, 7, 9\}$

**Set builder method:**

In this the common property of the elements is specified.

e.g. set A of all odd natural numbers less than 10.

$A = \{x : x \text{ is odd natural number less than } 10\}$

Symbols	Meaning
$\{ \}$	enclose elements in set
$\in$	belongs to
$\subseteq$	is a subset of (includes equal sets)
$\subset$	is a proper subset of
$\not\subset$	is not a subset of
$\supset$	is a superset of

## Kinds of Sets

- **Empty Sets or Null Sets** – sets with no elements.
  - **A = {girls in New York St. that have dicks}**
  - **A = { } or A =  $\emptyset$** . The set has 0 cardinality.
- **Infinite Sets** – sets with an infinite number of elements. Unlisted elements are denoted by ellipses.
  - **F = {x|x is a number}**
- **Finite Sets** – sets with an exact number of elements.
  - **H = {penises Chad has}**.  $n(H) = 27$ .

## The Power Set (P)

The power set is the set of all subsets that can be created from a given set.

*Example:*

$$A = \{a, b, c\}$$

$$\mathcal{P}(A) = \{\{a, b\}, \{a, c\}, \{b, c\}, \{a\}, \{b\}, \{c\}, A, \phi\}$$

## Cardinal Number of A Set

It is the number of elements in a set.

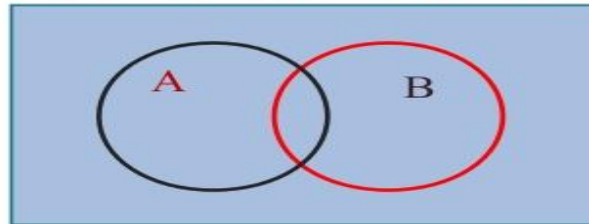
*Example:*

$$A = \{a, b, c, d\}$$

$$n(A) = 4$$

Representation of sets by means of diagrams known as:

## VENN DIAGRAM

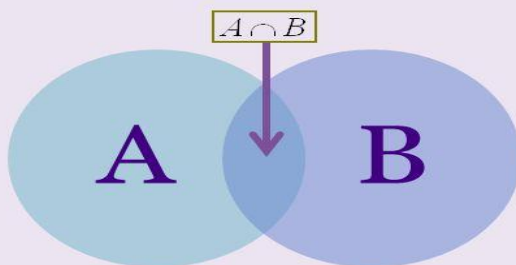


Venn Diagrams are named after the English logician, **John Venn**. These diagrams consist of rectangles and closed curves usually circles. The universal set is represented usually by a rectangle and its subsets by circles.

## Intersection and Union of Sets

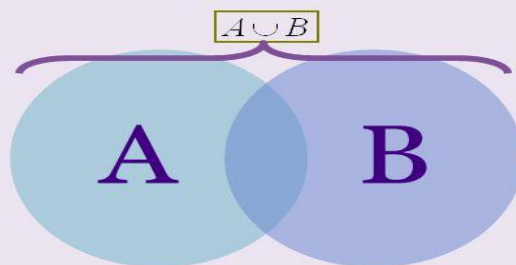
- **Intersection of Two Sets**

- The set containing only the elements that appear in both sets.
- ✦ Represented by the symbol  $\cap$ .



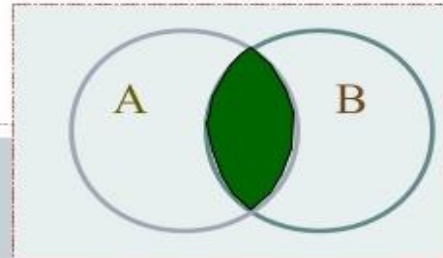
- **Union of Two Sets**

- The set containing all the elements found in either set.
- ✦ Represented by the symbol  $\cup$ .



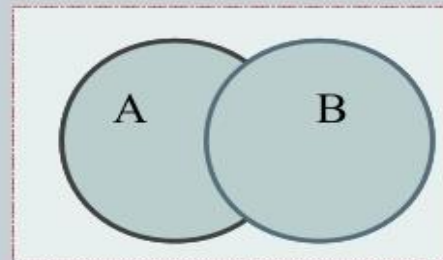
$$A \cap B$$

This is the intersect symbol. It means the set containing all elements that are in both A and B



$$A \cup B$$

This is the union symbol. It means the set that consists of all elements of set A and all elements of set B.



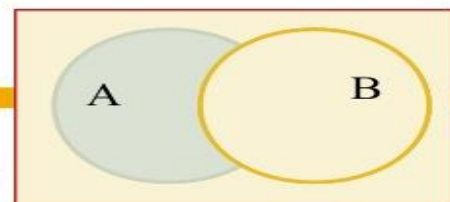
## Difference Of Sets

$$A - B$$

The difference of two sets A and B is the set of elements which belongs to A but which do not belong to B. It is denoted by  $A - B$ .

$$A - B = \{x : x \in A \text{ and } x \notin B\}$$

$$B - A = \{x : x \in B \text{ and } x \notin A\}$$



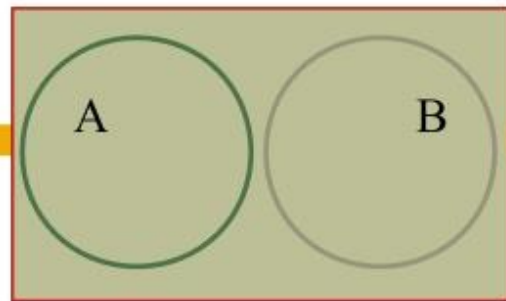
$$B - A$$



## Disjoint Sets

The two sets which do not have any elements in common are called disjoint sets.

$$A \cap B = \emptyset$$

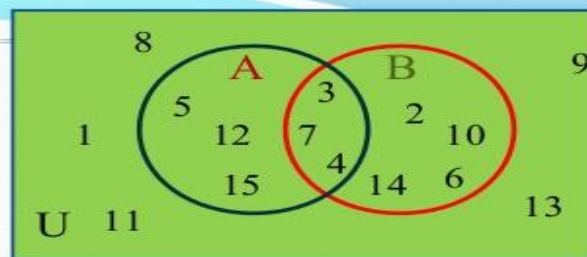
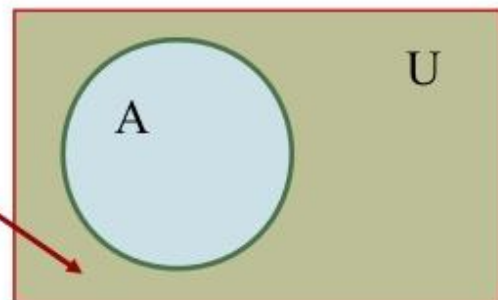


## Compliment of a set

If U is the universal set, A is a subset, then complement of A is

$$A^c = \{x: x \in U, x \notin A\}$$

$$\text{or } U - A$$



$$U = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15\}$$

$$A = \{3, 4, 5, 7, 12, 15\}$$

$$B = \{2, 3, 4, 6, 7, 10, 14\}$$

$$A \cap B = \{3, 7, 4\}$$

$$A \cup B = \{2, 3, 4, 5, 6, 7, 10, 12, 14, 15\}$$

$$A - B = \{5, 12, 15\}$$

$$B - A = \{2, 6, 10, 14\}$$

**VENN DIAGRAM**

**Commutative Laws:**

$$A \cap B = B \cap A \text{ and } A \cup B = B \cup A$$

**Associative Laws:**

$$(A \cap B) \cap C = A \cap (B \cap C) \text{ and } (A \cup B) \cup C = A \cup (B \cup C)$$

**Distributive Laws:**

$$A \cup (B \cap C) = (A \cup B) \cap (A \cup C) \text{ and } A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$$

**Double Complement Law:**

$$(A^c)^c = A$$

**De Morgan's Laws:**

$$(A \cap B)^c = A^c \cup B^c \text{ and } (A \cup B)^c = A^c \cap B^c$$

